

# A Double-Pendulum Robotic Platform to Understand Human Balance

## Project Proposal

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## Abstract

The following report is a project proposal for the development of a double pendulum robot that can be used by researchers to study controllers derived from human balance studies and by the COSMOS high school program for teaching about control systems. Ranking needs established that a device meeting the requirements for research would meet and exceed those of a device for teaching; Needs for a research device became the priority. Primary needs are an accurate human model, an easy to use interface, and accurate data acquisition. Specifications with the size specification of a 2 ft tall model and minimum perturbation distance of 5 in were the governing mechanical design factors. Two cart concept ideas recurred; The first a trackless cart and the second a cart on a track. Pendulum arm concepts also had a common theme of being directly driven by the actuator or having a transmission system. A preliminary 10 week schedule was established with milestones on the completion of the simulation, mechanical design package, calculations of the mechanics, and the design report. An initial calculation set a project budget estimate of \$500.

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# Introduction

The goal of the Double Pendulum Robotic Platform is to make a versatile robot that can be used to research human balance and to teach the basics of control systems to high school students. Inverted double pendulum systems are often used to study dynamics and control systems due to their chaotic behavior. The project is to use a double pendulum model to represent a human and use controllers to stabilize the chaotic dynamics caused by perturbations. In the scope of research, the robot will give researchers the ability to test the validity of different control system controllers on a physical model to better understand how human balance can be replicated in robots. As a teaching resource, the robot can be used by the COSMOS program to effectively engage students and demonstrate how control systems work. The goal is to have a fully functioning robot in addition to the appropriate documentation, programs, and interfaces to interact with the robotic system.

This report is a proposal to determine the scope of the Double Pendulum Robotic Platform project. The report provides an analysis of the results obtained from generating needs, preliminary specifications and concepts. It also outlines the preliminary project budget and a target schedule for the completion of the project.

## Mission Statement

<b>Product Description</b>	A double pendulum robot that can be perturbed by a specified motion and react based on a desired control system controller.
<b>Key Business Goals</b>	Ready for demonstration at the Senior Design Showcase
<b>Primary Market</b>	Researcher studying controllers for human balance COSMOS High School Instructor
<b>Secondary Market</b>	College Engineering Control Systems Instructor Robotics Researchers
<b>Assumptions</b>	Standalone Unit Computer Interfaced Safe to Operate
<b>Stakeholders</b>	User Project Sponsors COSMOS Program Organizers Manufacturers

## Project Needs

Professor Kong teaches COSMOS high school students how control system work during summer sessions. The current program allows students to input parameters into a single pendulum simulation programmed in MATLAB. Professor Kong would like a more engaging way for his students to learn about control systems. The double pendulum robot will do this by showing a physical control system simulation that his students can interact with.

The main goal is to give students a hands-on example of a control system. The device must be portable and easily stored because it will only be used during the summer program. Also, it should be easy to set so that the instructor can focus on helping his students rather than debugging the device. The device should have an interface that his students can use to input their result from the MatLab simulation and test it on a physical model. He would also like a way to allow students to collect data and generate plots. These are the basic needs for the COSMOS program.

In addition to the needs of Professor Kong, Dr. Moore is conducting research on human balance controllers and how humans react to perturbations. He would like a robot that can represent the human body, which will have two pendulums to represent leg and torso respectively. Main joints of the robot should have actuators to mimic torques applied on human's joints by muscles. The model needs to be physically similar to a real person, as well as changeable weight distributions with respect to different body types. This design should be able to achieve some basic controls, such as stand up and remain stable when perturbed by a platform.

As a research tool, the robot should have enough sensors to ensure the accuracy of the feedback controller and to collect data during simulations. The following data points need to be recorded: hip angle, ankle angle, and position of the robot. Pivot point should be able to provide a variable output holding torque that can be controlled directly by the controller.

## Preliminary Specifications

A set of specifications was created by the team to help guide the development of the design. A major specification governing the mechanical design of the system is the size of the unit. A preliminary decision was made to make a 2ft tall human model. This resulted in determining that the robot fit in a 2ft x 2ft x 2ft cube. Based on this sizing calculations for acceleration, velocity, and displacement distances could be established. A basic specification is to be able to simulate a person standing on an accelerating bus to 30 mph with a perturbation distance of 5 inches. After establishing a simulation more specifications will be created to determine torques and angles required for the mechanical assembly..

One need is the ease of setup. Several specifications were generated including using 110 VAC to power the power supply mains. For safety reasons DC voltage will be used to power the other components. This will allow the unit to be powered by any standard US outlet. In addition, the software should be plug and play with both Windows and UNIX based OS.

Necessary actuators and sensors need to be set to ensure the accuracy of the system. The experiments will be conducted under unstable environment, so a movable cart is a good choice. We can set the pendulums on the cart and achieve the basic controls and produce unstable environment by controlling the motion of the cart with respect to time. In this case, the location of the cart will be recorded, so the cart should be able to move freely without much friction. Meanwhile, the robot will also be used to educate high school students, so it should have a friendly human-machine interaction. Documentation and a guided tutorial are required to help users interact with the device. [Appendix C](#) has a list of various other specifications.

## Concept Generation

While existing solutions to the project were being researched, a brainstorming phase occurred simultaneously to generate many concepts to select from at a future time. This brainstorming phase began shortly after the specifications of our project were determined and is still ongoing. The goal of this phase is to come up with new ideas, to consider concepts that deviate from existing solutions, and to facilitate the discussion of possible issues. During this initial internal brainstorming phase, the project is separated into two sections – mechanical and software. While the software part is considered, the bulk of concept generation is focused on the mechanical side. Concepts were easy to generate when the mechanical portion is broken further into the cart, the pendulum, and electronics. The following will briefly describe the notable concepts while more concepts can be found in [Appendix D](#).

The only requirement for the cart is a platform that can travel along a determined motion path. Two concepts are especially notable based on simplicity and feasibility – the wheeled cart on a track and the trackless cart. A wheeled cart fitted with electric motors can easily produce a linear motion with accuracy of the motion increased by including a short track. This concept is basic, easily manufactured, and achieves the basic goal of the cart design. With a motor that will depend on the weight of the entire robot and on the magnitude of the desired forces, short, controlled perturbations can be generated. Attaching a sensor to the motor, using a servomotor, and using wheel encoders are all concepts developed to further elaborate on the wheeled cart since they all assist in recording data about the cart motion. This data can be used to fine-tune the cart motion to better achieve the desired pendulum perturbation.

The track cart concept is a platform fixed two two linear sliders and a ball screw or other actuator directing driving the motion of the cart. This cart concept allows for a steady, linear motion that is also easily controlled with the same sensors as the wheeled cart for fine-tuning. Although the concept incorporates a tougher design to manufacture, it is more capable of

preventing perturbations from the pendulum swing. Less noteworthy ideas mentioned include the usage of magnetism, pneumatic actuators to propel the car, or using an RC car.

The pendulum consists of two actuated arms representing a human body that can restore balance. Similarly to the cart, multiple ideas were brainstormed but there are two concepts that stood out. One method of actuating the pendulum arms is to simply attach servo motors at the joints. Considerations for this concept include a good wiring arrangement and placing a counterweight if the motors aren't centered. This concept is easy to manufacture and allows the joint to be directly actuated. The other notable concept is the use of drive belts to actuate the pendulum motion. Using drive belts eases the weight distribution of the arms because the motors will be on the cart body rather than the arms. The drive belt idea has further branched into two ideas based on the placement of the belts; the drive belts can be placed inside hollow arms for a more balanced rotation or on the outside of the arms for ease of manufacturing and repair. Other concepts for the pendulum arms that have been brought up is using a linear actuator in the form of a rack and pinion, electromagnets to control the weight distribution, and pins to also control the weight distribution.

The electronic system of the robot is likely the most important as it will collect the data and actuate the motion. Concepts discussed for this category involves the placement and type of sensors, method of data interpretation, control of inputs to the motors and control system, and the collection of outputs like holding torque. Sensors for the cart to determine the acceleration can be rotary encoders, accelerometers, or a laser positioning system. For the pendulum arms, accelerometers and gyroscopes can be used to track the angular acceleration. A microcontroller can control all the robot functions or a network connection can be used to control the robot remotely. A PLC is also discussed as an alternative to control the robot function. The data collected from the sensors has been discussed to be collected via an SD card or sent over Wi-Fi.

## Preliminary Budget

This project uses a mixture of mechanical and electrical parts. The mechanical parts include the materials used to build the cart and the pendulum arms; a ball screw or three drive belts; a set of four wheels; and a track or rail system. Electrical components include the accelerometer, rotary encoders, microcontroller, and the two actuators. There are also some other miscellaneous expenses that will be used to manufacture the robot. The sum total of a set of parts that constitute a complete robot (cart, pendulum, sensors, actuators) comes out to be about \$500. [Appendix H](#) shows the complete breakdown of the estimated costs, including variations of part concepts.

## Preliminary Schedule

In order to meet the project requirements in the given time frame, a preliminary schedule has been created. The first three weeks of the group's formation is spent laying the groundwork for

the rest of the project. This includes getting to know one another, everyone's schedule, building the team charter, identifying the mission statement, and creating a list of needs and specifications. The next couple of weeks have a focus on concept generation. This leads to the present, or week six of the project, where more concept generation will overlap with the start concept selection. For the concept selection, there will be approximately a week to select everyone's favorite concepts and make combinations of concepts to start conceptualizing the design. Simultaneously, selection criteria will be created, followed by calculations to rank the concepts accordingly. A third major objective during these upcoming weeks alongside concept selection is the completion of the simulation. The simulation will assist in choosing the best concepts while the concepts will guide what the simulation will model. While the criteria will be accomplished by next week, the selection and simulation will be completed at the beginning of March. This leaves the rest of the quarter to fully develop and flesh out the design chosen from the concepts.

Next quarter is dedicated to the implementation of the design. The first week and a half of the quarter will be spent following up and ensuring quality CAD models and drawings so machining and construction can proceed smoothly. Half the team will begin construction of each of the subcategories (cart, pendulum, framework) immediately after the drawings are completed. The other half will fully design the control systems and programming of the control software. Around the time the control systems are ready to be implemented, the robot should be completed and the full team will be available to complete the physical portion of the project. This is followed by testing and documentation. A Gantt chart can be found in [Appendix I](#).

## Conclusion

This report established the scope of the Double Pendulum Robot Platform and provided a brief outline for the implementation of the project. The needs of the project were defined and it was determined that the needs for researchers outweighed those of the teaching robot. Several preliminary specifications were created with the overall size of a 2ft scaled model of the unit governing many of the other specifications. Concepts for the mechanical design of the cart emphasized a trackless cart design and a tracked cart on sliders. The pendulum designs allow for actuation by different means either directly at the pivot points or by transmission through gearing or drive belts. The preliminary project budget is \$500 but may increase based on the concept selection. The team plans to complete a CAD package and documentation by the end of this quarter and implement the project next quarter.

# Appendices

## Appendix A: Stakeholders

List of project stakeholders

Stakeholder	Relation to Project
Sponsors	Primary funders and supporters of the project.
High School Students	Will benefit from learning about control systems.
COSMOS Instructor	Be able to effectively engage and teach students about control systems.
Robotics Researchers	Verify controllers that define human balance and use data in robotics.
Prosthetics Industry	Understand balance better and develop better prosthetics.
Programmers	Have to be able to control and provide interface for robot to users.
Manufacturers	Robot must be manufacturable.

## Appendix B: Needs

The following are a list of needs that were determined by the stakeholders and team.

#	Needs	Rank
<b>1</b>	<b>Controller must be easy to make modifications to.</b>	<b>5</b>
a	<i>Controller must allow for different controllers to be inputted.</i>	
b	<i>Allow for various gains and parameter changes.</i>	
c	<i>Easy upload of simulations data.</i>	
<b>2</b>	<b>Robot must be able to represent human physiology</b>	<b>10</b>
a	<i>The pendulum should be able to bend like a human.</i>	
b	<i>The pendulum weight distribution should be easy to change.</i>	
<b>3</b>	<b>Pendulum should be able to recover from tipping over.</b>	<b>11</b>
a	<i>A steady state position should be able to be established.</i>	
b	<i>Should react to relatively controlled perturbations.</i>	



<b>4</b>	<b>The robot should be easy to setup.</b>	<b>3</b>
a	<i>Will not break when moving.</i>	
b	<i>Easy to interface with.</i>	
c	<i>Be portable and easy to move.</i>	
d	<i>Be convenient to power</i>	
<b>5</b>	<b>Collect data in a way that can be used for analysis</b>	<b>7</b>
a	Easy to download data.	
b	Provide readings of each sensor in appropriate intervals.	
c	Provide data on robot reactions.	
d	Have sensors on each linkage.	
<b>6</b>	<b>Must be easy to manufacture</b>	<b>8</b>
a	Custom parts easy to make.	
b	<i>Simpler model that will interface with the robot.</i>	
c	As many off the shelf parts as possible.	
<b>7</b>	<b>Should be economically affordable</b>	<b>4</b>
a	Use as many inexpensive parts as possible.	
b	Manufacturing processes should be easy to conduct.	
<b>8</b>	<b>Tests should be repeatable.</b>	<b>6</b>
a	<i>Robot should be able to reset itself after each test.</i>	
b	<i>Perturbations should be able to be repeatable.</i>	
<b>9</b>	<b>Robot should be easy to maintain</b>	<b>9</b>
a	<i>Should be able to withstand daily wear and tear.</i>	
b	<i>Have a maintenance guide.</i>	
c	<i>Use as many off the shelf and easy to replace parts.</i>	

<b>10</b>	<b>Must be engaging for high school students.</b>	<b>2</b>
a	<i>Easy to use interactive interface.</i>	
b	<i>Simpler model that will interface with the robot.</i>	
<b>11</b>	<b>Must be safe to use</b>	<b>1</b>
a	<i>Limit damage caused by arm.</i>	
b	<i>Be electrically safe.</i>	

## Appendix C: Target Specifications

#	Need #	Description of Specification	Units
1	1, 8	Connect with a single click.	clicks
2	1, 5, 8	Interface with a windows PC.	N/A
3	1	Process a human readable control equation.	N/A
4	2	Robot must be 2ft tall.	ft
5	2	Robot must have 3 different weight configurations.	lbf/in
6	2	1st pendulum should have 180 degree motion.	degree
7	2	2nd pendulum should have 270 degree motion.	degree
8	2	Minimum Torques should be the maximum joint torques of a human.	lbf-in
9	3, 6	Use less than 150 parts.	parts
10	3	Maintenance Manual no bigger than 5 pages.	pages
11	3,6	Use less than 20 custom parts.	parts
12	4	Cart should record velocity.	in/s
13	4	Distance traveled accuracy +/- 0.125 inches.	in
14	4	Sensors accuracy +/- 0.125 inches.	inches
15	4	Max Travel Distance of 5 inches.	in

16	4	Min velocity 50 in/sec.	in/s
17	4	Min Acceleration 80 in/sec <sup>2</sup>	in/s <sup>2</sup>
18	5	3 clicks to download data files.	clicks
19	5, 9	Have at least one sensor per linkage.	sensors
20	5	Store data to csv file.	format
21	5	Take readings of all sensors at least every 10ms.	ms
22	5	Sensors accuracy 0.5 degrees.	degrees
23	6	HMI with less than 10 inputs.	inputs
24	6	Graphically Appealing.	subj
25	6	Defined control equation that parameters can be changed.	equation
26	7	Pad robotic arm with Shore 40 or less.	Shore
27	7	Ground Robot.	N/A
28	7	Use 24 VDC.	V
29	7	Have E-Stop.	N/A
31	8	Default control equation.	equation
32	9	Cart should record velocity.	in/s
33	9	Distance traveled accuracy +/- 0.125 inches.	in
34	9	Max Travel Distance of 5 inches.	in
35	9	Min velocity 50 in/sec.	in/s
36	9	Min Acceleration 80 in/sec <sup>2</sup>	in/s <sup>2</sup>
37	9	Sensors accuracy +/- 0.125 inches.	inches

## Appendix D: Internal Concepts

Category	Description	Category	Description
Cart		Sensors	

Motion	Build a ramp or slide of varying height.	Physical	Placed next to each actuator
	Electric or pneumatic motors.		Placed at the center of gravity of each arm and on the cart
	Earthquake shake table for uncontrolled perturbations		Placed on opposite ends of each legs
	Magnetic pulses to send cart down a track		Single sensor per arm
	Circular track for continuous motion		Multiple sensor per arm
	Solenoid actuators		Sensors are placed in the middle of an arm
	Belt driven motor on a track		Rotary encoder to track cart distance and angular rotation
	Place pendulum on an RC car		Accelerometer for cart
	Ball screw to drive the motion		Gyroscope for pendulum arms
	Rocket propellant		Camera to measure angle of the linkage
	Water based track to float the cart		GPS to analyze location and relative movement
	Giant fan/propeller		Giant touchscreen and stylus system
	Stepper motor	Software	Connect via serial
	Feedback control system		Connect via Bluetooth
Materials	Lightweight to reduce motor power		Connect via Wifi
	Heavy to reduce effect of perturbations from the pendulum		Make an onboard server to access with wifi
	Durable material		Screen and keyboard connected to robot directly
	Cheap		HMI
	Easy to build with		Interpret equations then send to microcontroller
Control	GPS positioning		Microcontroller handles calculations of inputs and outputs
	Wifi positioning		PLC to control main functions

	Colored track to measure distance traveled		Telnet/Remote control
	Microcontroller to control time traveled		Log data on to an SD card
	Laser pointer to calculate distance		Log into a wifi server
	Rotary encoders		Pictures of data are printed out
			Binary printout using LEDs
Pendulum			Angle, current, torque, and time are measured
Weight	Sliding weights to adjust the distribution/center of mass		
	Pins/pegs at regular intervals		
	Electromagnet to generate a weight force		
	Hollowed arms filled with a fluid		
	Hooks used to hang weights		
	Solar sails to generate a weight force		
	Upper arm is shorter than lower arm		
	Upper arm weighs more than lower arm		
Balance	Actuators on the ends of each arm		
	Actuators both on the cart		
	Linear actuator to drive a rack and pinion		
	Drive belts to move each arm		
	Fan propellers to rotate the arm		
	Letting the pendulum swing around with a movable weight (controlled) to rebalance		
	Limit range of motion to simulate a human's range of motion		
	Drive belts can be external		

## Appendix E: External Concepts Research

External research the team did on the various subcategories.

<b>Cart</b>	
Misumi Linear Drive Screw - Basic Leadscrew system that can be purchased.	<a href="https://us.misumi-ec.com/vona2/detail/110300076760/?Inch=0">https://us.misumi-ec.com/vona2/detail/110300076760/?Inch=0</a>
Misumi Belt Drive - Basic belt driven system.	<a href="https://us.misumi-ec.com/vona2/detail/110302499820/?Inch=0">https://us.misumi-ec.com/vona2/detail/110302499820/?Inch=0</a>
Video of Double Pendulum Cart - Demonstrating swing up and balance	<a href="https://www.youtube.com/watch?v=B6vr1x6KDaY">https://www.youtube.com/watch?v=B6vr1x6KDaY</a>
Quanser Double Pendulum Cart - Lab equipment	<a href="http://www.quanser.com/Search.aspx?q=double%20pendulum">http://www.quanser.com/Search.aspx?q=double%20pendulum</a>
Emotimo - Camera Motion Control	<a href="http://emotimo.com/ifootage/">http://emotimo.com/ifootage/</a>
Camera Slider	<a href="https://sites.google.com/site/3dprinterlist/other-machines/simple-camera-slider">https://sites.google.com/site/3dprinterlist/other-machines/simple-camera-slider</a>
Aliexpress Slider Bearings and track	<a href="http://www.aliexpress.com/item-img/MGNR9-L-400mm-HIWIN-9mm-Miniature-Linear-Guide-Rail-MGNR9R400CM-MGN9-MGN/1909388138.html">http://www.aliexpress.com/item-img/MGNR9-L-400mm-HIWIN-9mm-Miniature-Linear-Guide-Rail-MGNR9R400CM-MGN9-MGN/1909388138.html</a>
Reprap - Open Source 3d printer (linear stage)	<a href="http://reprap.org/">http://reprap.org/</a>

<b>Sensors</b>	
Sparkfun Rotary Encoder	<a href="https://www.sparkfun.com/products/10932">https://www.sparkfun.com/products/10932</a>
Gyroscope Sensor	<a href="http://www5.epsondevice.com/en/information/technical_info/gyro/">http://www5.epsondevice.com/en/information/technical_info/gyro/</a>
Accelerometer Sensor	<a href="https://www.adafruit.com/products/439?gclid=CLzcoODf89ECFQx9fgodhqYJxQ">https://www.adafruit.com/products/439?gclid=CLzcoODf89ECFQx9fgodhqYJxQ</a>
Accelerometer Sensor - Description	<a href="https://www.dimensionengineering.com/info/accelerometers">https://www.dimensionengineering.com/info/accelerometers</a>
Ultrasonic	<a href="https://www.bananarobotics.com/shop/HC-SR04-Ultrasonic-Distance-Sensor?gclid=COjN-6Xg89ECFQ9Efgod5sgMvw">https://www.bananarobotics.com/shop/HC-SR04-Ultrasonic-Distance-Sensor?gclid=COjN-6Xg89ECFQ9Efgod5sgMvw</a>
IR sensor	<a href="http://www.trossenrobotics.com/c/robot-IR-sensors.aspx">http://www.trossenrobotics.com/c/robot-IR-sensors.aspx</a>

<b>Actuators</b>	
Stepper Motor	<a href="https://en.wikipedia.org/wiki/Stepper_motor">https://en.wikipedia.org/wiki/Stepper_motor</a>
Brushless DC Motor	<a href="https://en.wikipedia.org/wiki/Brushless_DC_elect ric_motor">https://en.wikipedia.org/wiki/Brushless_DC_elect ric_motor</a>
Hydraulic Rotary Actuator	<a href="http://ph.parker.com/us/en/hydraulic-rotary-actuators">http://ph.parker.com/us/en/hydraulic-rotary-actuators</a>
Drive Belts	<a href="http://sdp-si.com/products/timing-belts/gt2.php">http://sdp-si.com/products/timing-belts/gt2.php</a>
Pneumatic rotary actuator	<a href="http://ph.parker.com/us/en/pneumatic-rotary-actuator-prn-series-vane">http://ph.parker.com/us/en/pneumatic-rotary-actuator-prn-series-vane</a>
SMC rotary pneumatic actuator	<a href="http://www.smcetech.com/CC_host/pages/custom/templates/smc_v2/prodtree_branch_group_2.cfm?cc_nv1=((CC,smc,ACT_US,Node_20136))&amp;CFID=14844630&amp;CFTOKEN=48021297&amp;jsessionid=84304c83f0811ff741e62b567e16251c732c">http://www.smcetech.com/CC_host/pages/custom/templates/smc_v2/prodtree_branch_group_2.cfm?cc_nv1=((CC,smc,ACT_US,Node_20136))&amp;CFID=14844630&amp;CFTOKEN=48021297&amp;jsessionid=84304c83f0811ff741e62b567e16251c732c</a>
DC Motor Stall Torque	<a href="http://lancet.mit.edu/motors/motors3.html">http://lancet.mit.edu/motors/motors3.html</a>
DC Motor Torque	<a href="http://fab.cba.mit.edu/classes/961.04/topics/speed_torquecurve.pdf">http://fab.cba.mit.edu/classes/961.04/topics/speed_torquecurve.pdf</a>
Pneumatic Artificial Muscles	<a href="https://en.wikipedia.org/wiki/Pneumatic_artificial_muscles">https://en.wikipedia.org/wiki/Pneumatic_artificial_muscles</a>

<b>Double Pendulum</b>	
Double Pendulum demonstration using single actuator	<a href="http://www.pendcon.de/double-pendulum.html">http://www.pendcon.de/double-pendulum.html</a>
Double pendulum - Research of chaotic behavior of double pendulum.	<a href="http://www.noise.physx.u-szeged.hu/Research/DoublePendulum/">http://www.noise.physx.u-szeged.hu/Research/DoublePendulum/</a>
US Patent - Drive system for multiple axis robot arm	<a href="https://www.google.com/patents/US6601468">https://www.google.com/patents/US6601468</a>
US Patent- Methods and systems for double-pendulum crane control	<a href="https://www.google.com/patents/US8235229">https://www.google.com/patents/US8235229</a>
Double Pendulum - CAD Model	<a href="https://grabcad.com/library/double-pendulum?locale=ru">https://grabcad.com/library/double-pendulum?locale=ru</a>

Double Pendulum Video - Free moving	<a href="https://www.youtube.com/watch?v=pYPRnxS6uAw">https://www.youtube.com/watch?v=pYPRnxS6uAw</a>
Double Pendulum Research - Motion of Double Pendulum	<a href="http://digitalcommons.calpoly.edu/cgi/viewcontent.cgi?article=1059&amp;context=physsp">http://digitalcommons.calpoly.edu/cgi/viewcontent.cgi?article=1059&amp;context=physsp</a>
US Patent - Robot Arm System	<a href="https://www.google.com/patents/US20120048047">https://www.google.com/patents/US20120048047</a>

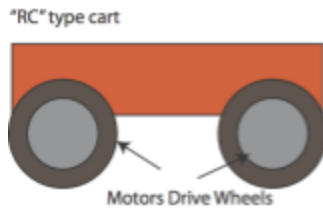
<b>Controllers</b>	
Velocio PLC - Cheap PLC	<a href="http://velocio.net/ace/">http://velocio.net/ace/</a>
Beaglebone - Linux, GPIO, Analog, Ethernet	<a href="https://beagleboard.org/black">https://beagleboard.org/black</a>
Arduino - Analog, Digital IO, Serial I2C	<a href="https://store-usa.arduino.cc/products/a000066">https://store-usa.arduino.cc/products/a000066</a>
Raspberry PI - Wifi, Ethernet, GPIO, Serial	<a href="https://www.raspberrypi.org/products/raspberry-pi-3-model-b/">https://www.raspberrypi.org/products/raspberry-pi-3-model-b/</a>
Current Limiter	<a href="http://www.mouser.com/ProductDetail/Texas-Instruments/TPD3S014DBVR/?qs=1CfNGUMoiQ%252bDmiZShdIX0g%3D%3D&amp;gclid=CNrerJ3e89ECFUdufgodTWIFgg">http://www.mouser.com/ProductDetail/Texas-Instruments/TPD3S014DBVR/?qs=1CfNGUMoiQ%252bDmiZShdIX0g%3D%3D&amp;gclid=CNrerJ3e89ECFUdufgodTWIFgg</a>
Digital Potentiometer	<a href="http://www.newark.com/microchip/mcp41010-i-p/digital-potentiometer-10kohm-256/dp/69K7607?mckv=IJB3Mec1&amp;gross_price=true&amp;CATCI=pla-164506470981&amp;CAAGID=20389674261&amp;CMP=KNC-GUSA-GEN-SHOPPING-69K7607&amp;CAGPSPN=pla&amp;gclid=CLPNrLXe89ECFYFYfgod0g4ArQ&amp;CAWELAIID=120185550001160034">http://www.newark.com/microchip/mcp41010-i-p/digital-potentiometer-10kohm-256/dp/69K7607?mckv=IJB3Mec1&amp;gross_price=true&amp;CATCI=pla-164506470981&amp;CAAGID=20389674261&amp;CMP=KNC-GUSA-GEN-SHOPPING-69K7607&amp;CAGPSPN=pla&amp;gclid=CLPNrLXe89ECFYFYfgod0g4ArQ&amp;CAWELAIID=120185550001160034</a>
Sparkfun Motor Driver	<a href="https://www.sparkfun.com/products/13911">https://www.sparkfun.com/products/13911</a>
Pololu Stepper Motor Driver	<a href="https://www.pololu.com/category/120/stepper-motor-drivers">https://www.pololu.com/category/120/stepper-motor-drivers</a>



## Appendix F: Internally Generated Cart Concepts Revisited

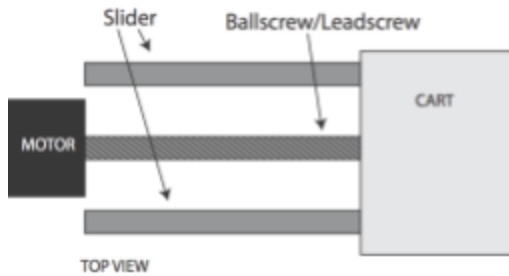
The following concepts were generated after the initial concepts generation session and external research discussions. These three ideas show a more refined development of a combination of ideas that came from these sessions.

### Trackless Design



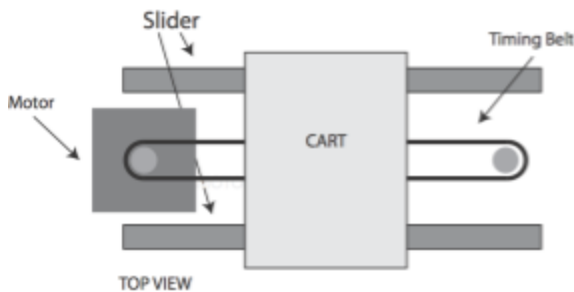
**Figure 2:** This initial concept is a trackless design that uses motors to drive the cart. One pitfall is the lack of accurate positional control.

### Leadscrew/Ballscrew Design



**Figure 3:** This is an initial track design using a leadscrew or ballscrew. This allows for great positional accuracy as well as a lower weight for the motor to move.

### Belt Drive Design

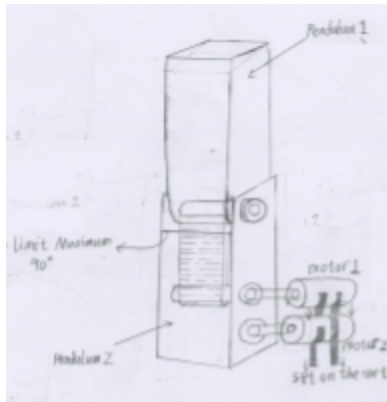


**Figure 4:** This is a belt driven track design. This provides a relatively good positional accuracy and is cheap.

## Appendix G: Internally Generated Pendulum Concepts

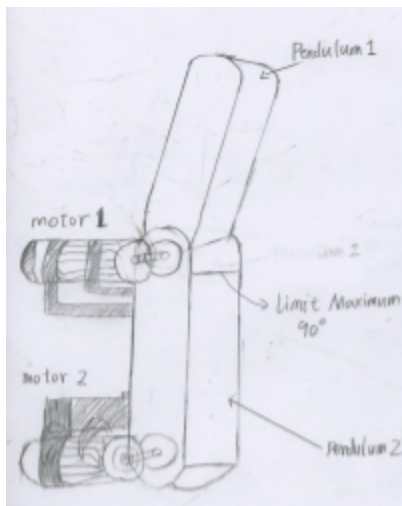
These are the three refined designs that were developed after the initial concepts and external research.

### Internal Belt Drive



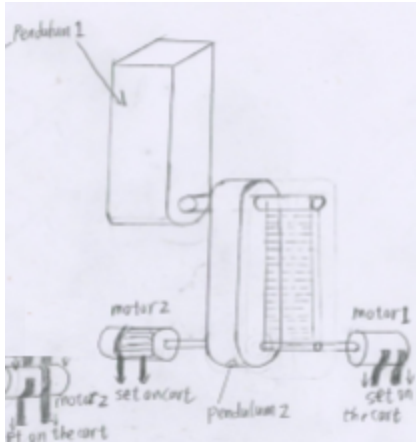
**Figure 5:** The motors are rigidly attached to the base. Motor 1 applies energy to the top link by a chain or belt inside the bottom link.

### Direct Motor Mount



**Figure 6:** Motors are externally attached to the pivot points in both linkages rather than being transferred via a belt.

## External Belt Drive



**Figure 7:** Both motors are rigidly attached to the cart base. Torque is transferred to the upper link through the belt/chain attached externally.

## Appendix H: Budget

Please note budget is very rough. Yellow indicates a decision needs to be made.

Part	Quantity	Cost	Subtotal
Cart	1	\$20	\$20
Bearings	4	\$10	\$40
Drive Belt	3	\$15	\$45
Track	1	\$50	\$50
Pendulum arm	2	\$30	\$60
Accelerometer	2	\$18	\$36
Rotary Encoder	3	\$30	\$90
Motor - pneumatic	2	\$65.00	\$130
Motor - electric	2	\$38	\$75
Microcontroller	1	\$50	\$50
Total (for a complete subsystem):			~ \$500

# Appendix I: Gantt Chart

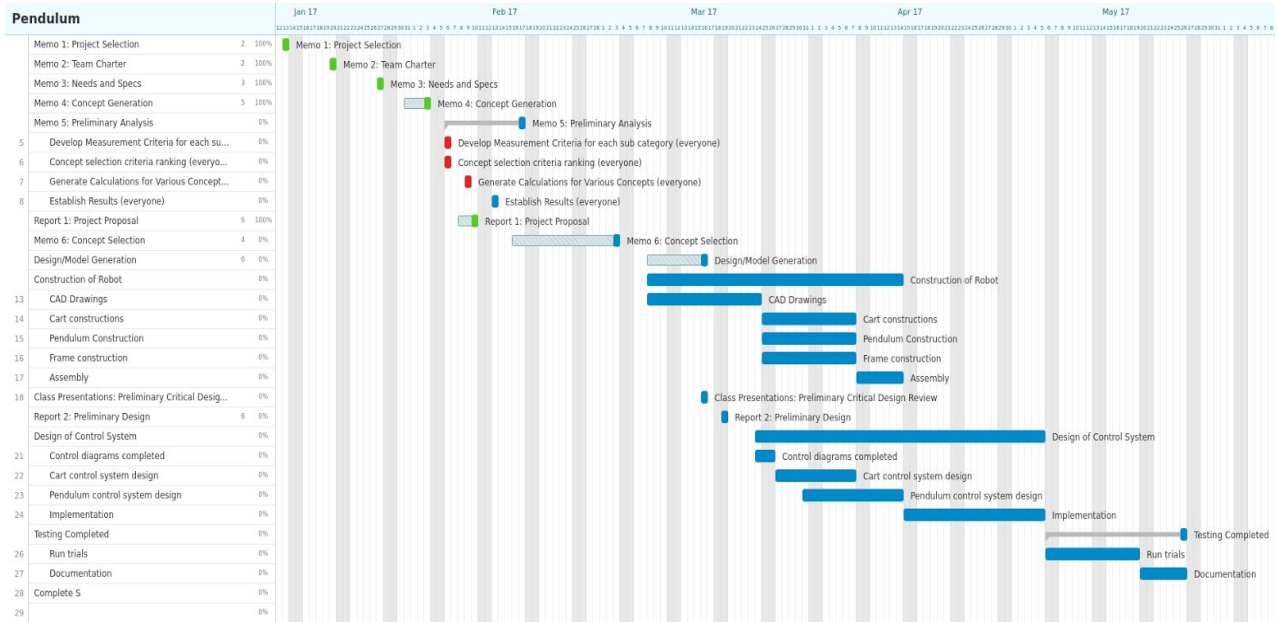


Figure 8. Complete Gantt chart for weeks 1 through 20. (Legend: green - completed tasks, red - late tasks, blue - upcoming tasks)